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## Demand-Supply Interactions on Future Mining Resources Production: The Coal Model



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# Resource Supply Considerations



- How much of it exists? (discovery)
  - How much is recoverable?
  - When is it recovered?
  - How fast can it be recovered?
- 
- What market is it supplying?
  - What is the demand?
  - How long will it last?

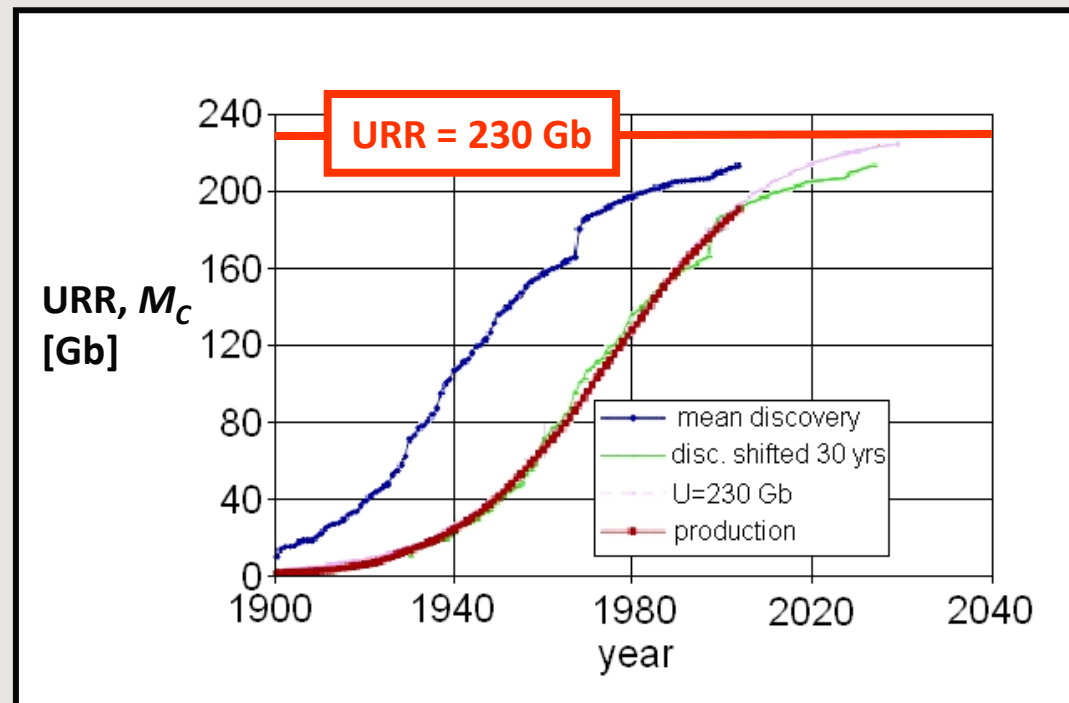
What is the interaction between demand and supply with limited resource?

# URR – Ultimately Recoverable Resources



- Total amount of a resource that can be extracted.
- Increase with time as discoveries are made.
- Follows a Sigmoidal curve.

- Example: USA  
URR and  
cum. prod.,  $M_C$



# Annual Production (Hubbert's Curve)



- Annual production assumed to follow a bell curve.
- Given by the gradient of the cumulative production curve:

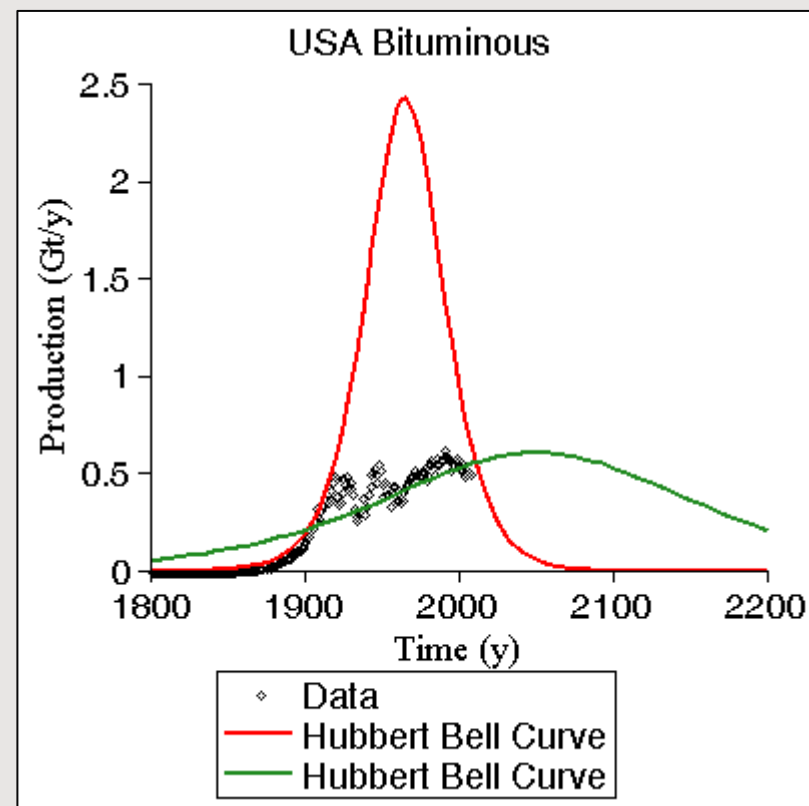
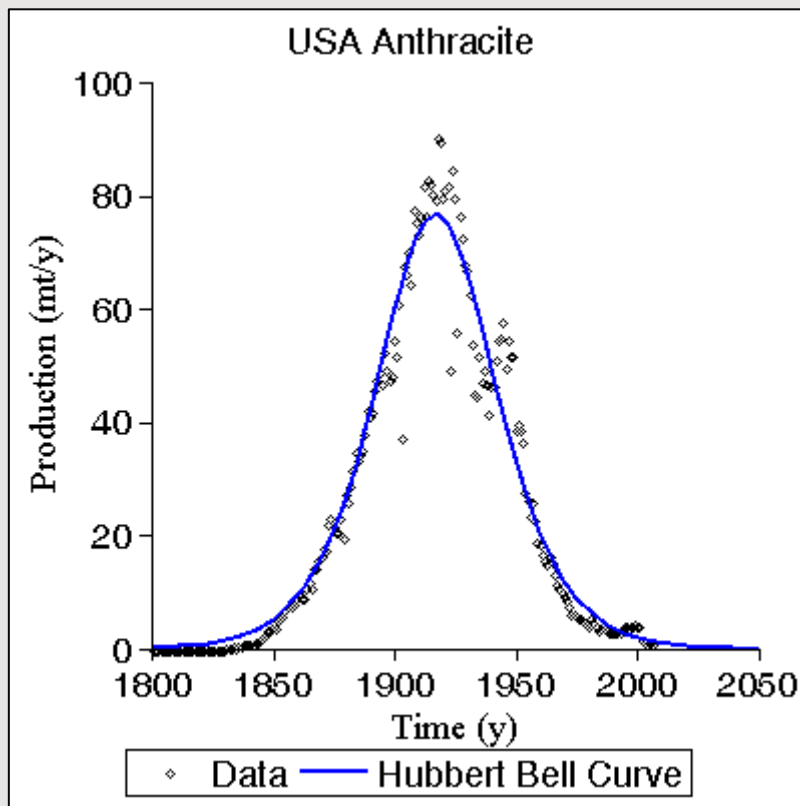
$$M_s[t] = \frac{dM_c}{dt} = rURR \left[ \frac{e^{r(t-t_p)}}{\left(1 + e^{r(t-t_p)}\right)^2} \right]$$

$r$  rate constant ( $y^{-1}$ )

$t_p$  peak year (y)

# Does Hubbert's Curve always apply?

- Both for the USA (anthracite and bituminous).
- Two curves (before and after WW1) for bituminous.

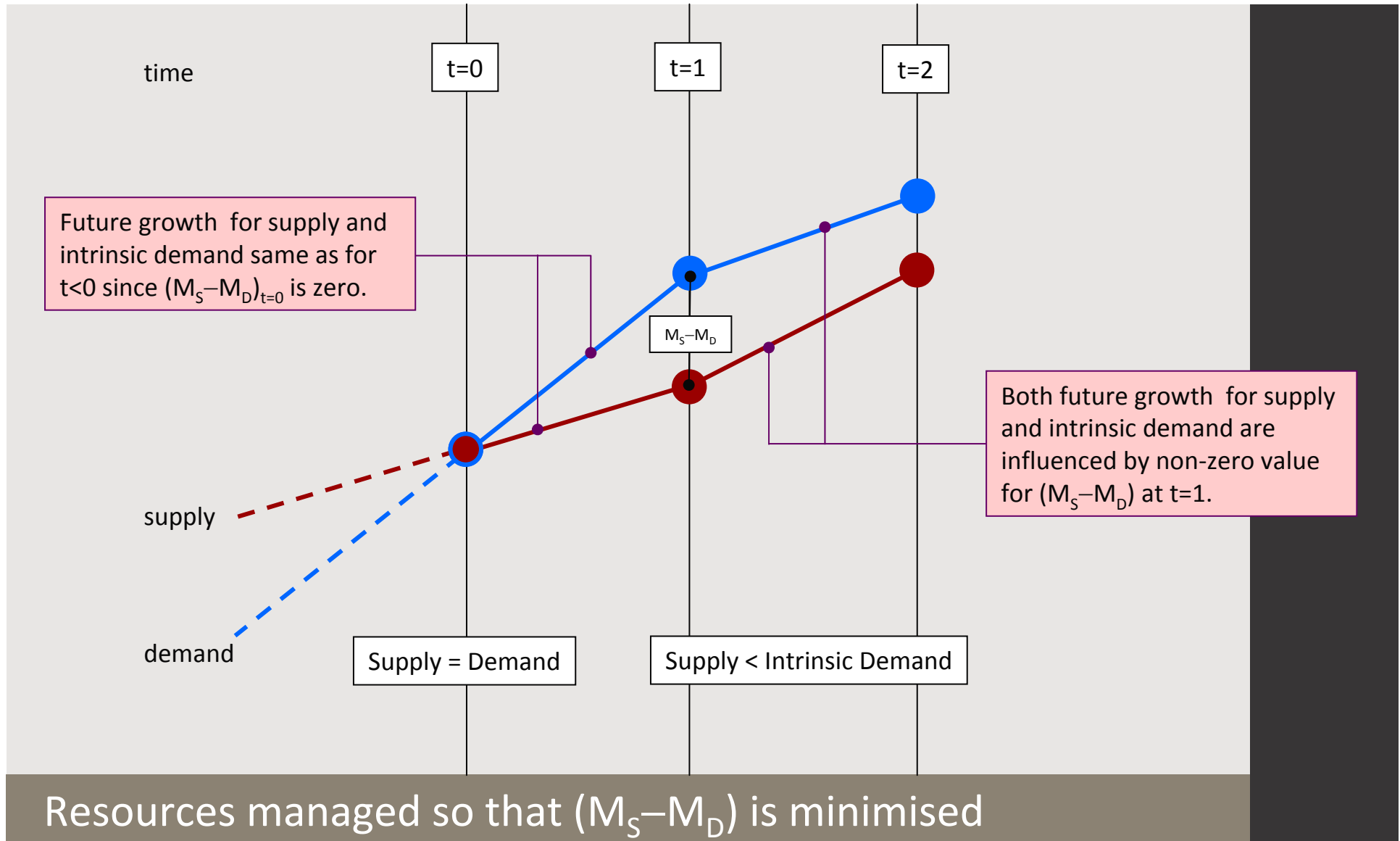


# Demand-Supply Model



- Based on an identified market for a resource.
- Estimate the URR of the resource for that market.
- Assume production capacity for each operation needed to extract the resource. From URR, gives the total number of operations.
- For each year, operations are brought online, operated at steady state or upgraded, and taken off-line, so that supply meets intrinsic demand.
- If intrinsic demand is greater than supply then intrinsic demand is reduced and supply increased (if capacity allows it) for the following year.

# Supply-Demand Interaction



# Intrinsic Demand

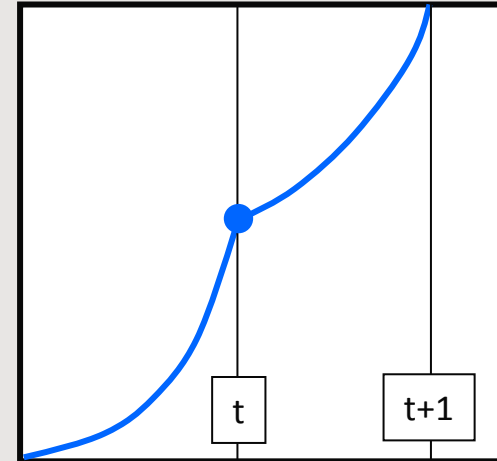
- Exponential growth

$$M_D[t+1] = M_D[t]e^{k_D[t]}$$

- Demand exponent coefficient updated for each time period

$$k_D[t] = k_{D0} - k_1 \left( \frac{M_S[t] - M_D[t]}{M_S[t]} \right)$$

$M_S[t] - M_D[t]$  market driver  
 $k_{D0}$  and  $k_1$  constants

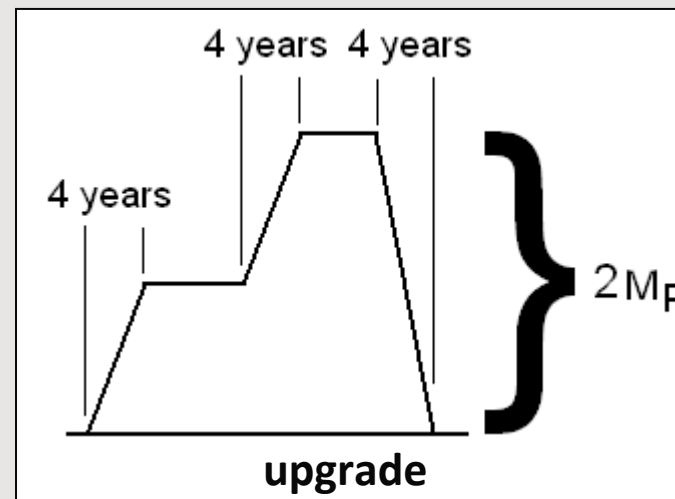
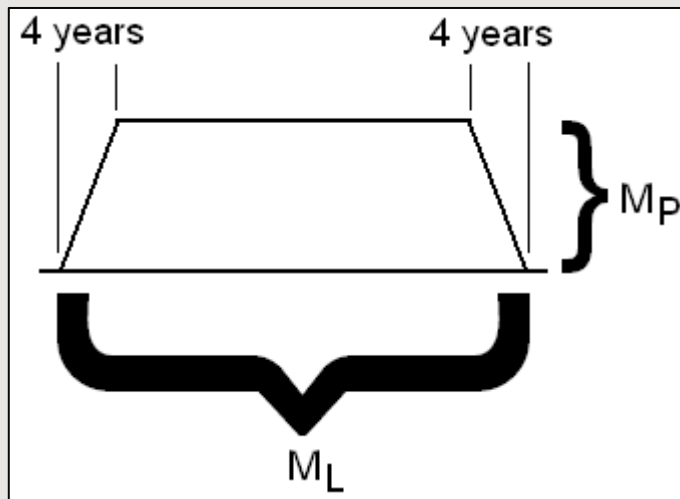


# Supply

- Sum of production from each source (mine)

$$M_S[t + 1] = \sum_{j=1}^M P^j[t + 1]$$

- Source production schedule



**Sources automatically brought on-line, off-line, upgraded**

# Sources Online



$$M[t + 1] = \left[ M_T - (M_T - M[t]) e^{-k_s[t] \frac{M_s[t]}{URR}} \right]$$

$M_T$  Total number of sources

$k_s[t]$  Supply exponent coefficient

$$k_s[t] = k_{s0} + k_2 \left( \frac{M_s[t] - M_D[t]}{M_s[t]} \right)$$

$M_s[t] - M_D[t]$  market driver

$k_{s0}$  and  $k_2$  constants

# Source Increased Production (Upgrade)



- When (normalised) if the supply-demand gap is greater than a set value then source production is upgraded:

$$M_U[t + 1] = \left[ k_3 \left( \frac{M_S[t] - M_D[t]}{M_S[t]} - k_U \right) M[t] \right]$$

$k_U$	normalised limit for upgrade
$M_S[t] - M_D[t]$	market driver
$k_3$	proportionality constant

In addition to sources being brought online

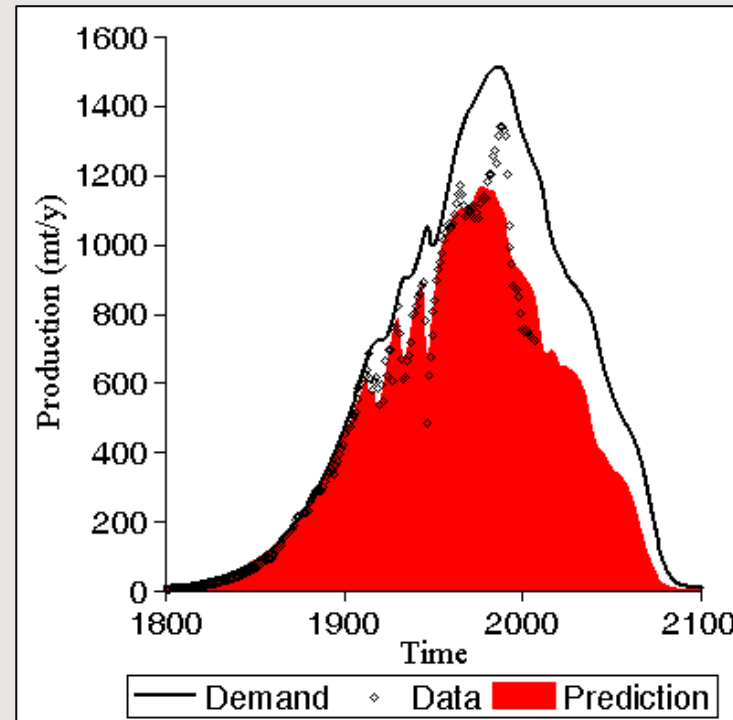
# Demand-Supply Coal for Oceania



Type	URR (Gt)
Bituminous	51
Sub-bituminous	3
Lignite	40
Other	1
<b>Total</b>	<b>95</b>

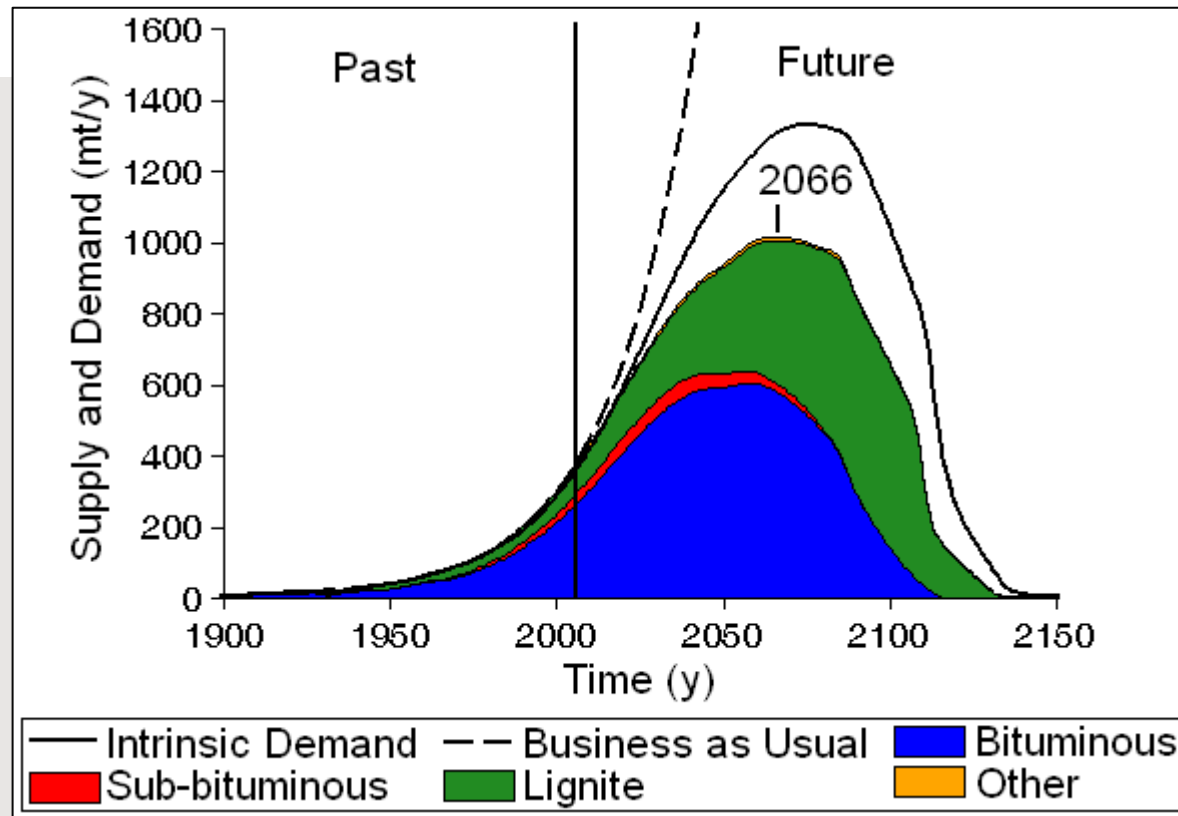
- Average mine production is 0.84 Mt/y
- Total number of mines,  $M_T$ , is 1450

# Demand-Supply Constants



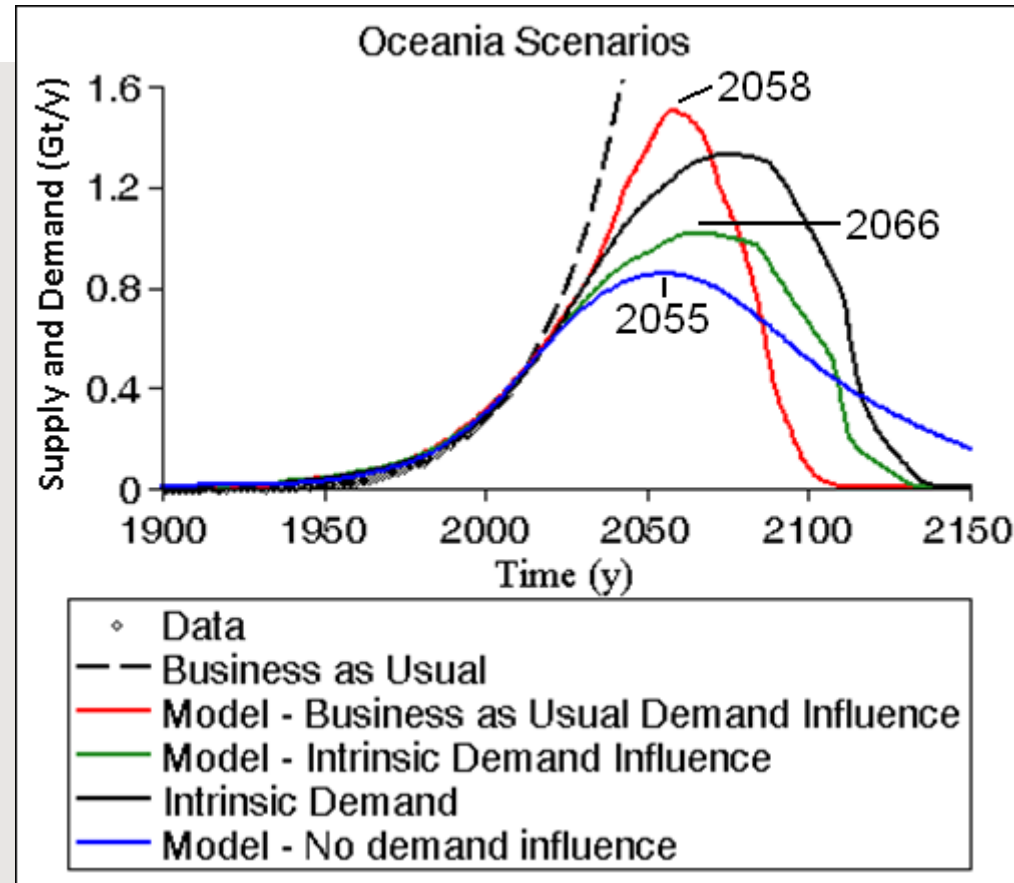
- Based on European coal Market (peaked in 1980's)
- Regression to get values for  $k_1, k_2, k_3, k_U$

# Demand-Supply: Oceania Coal



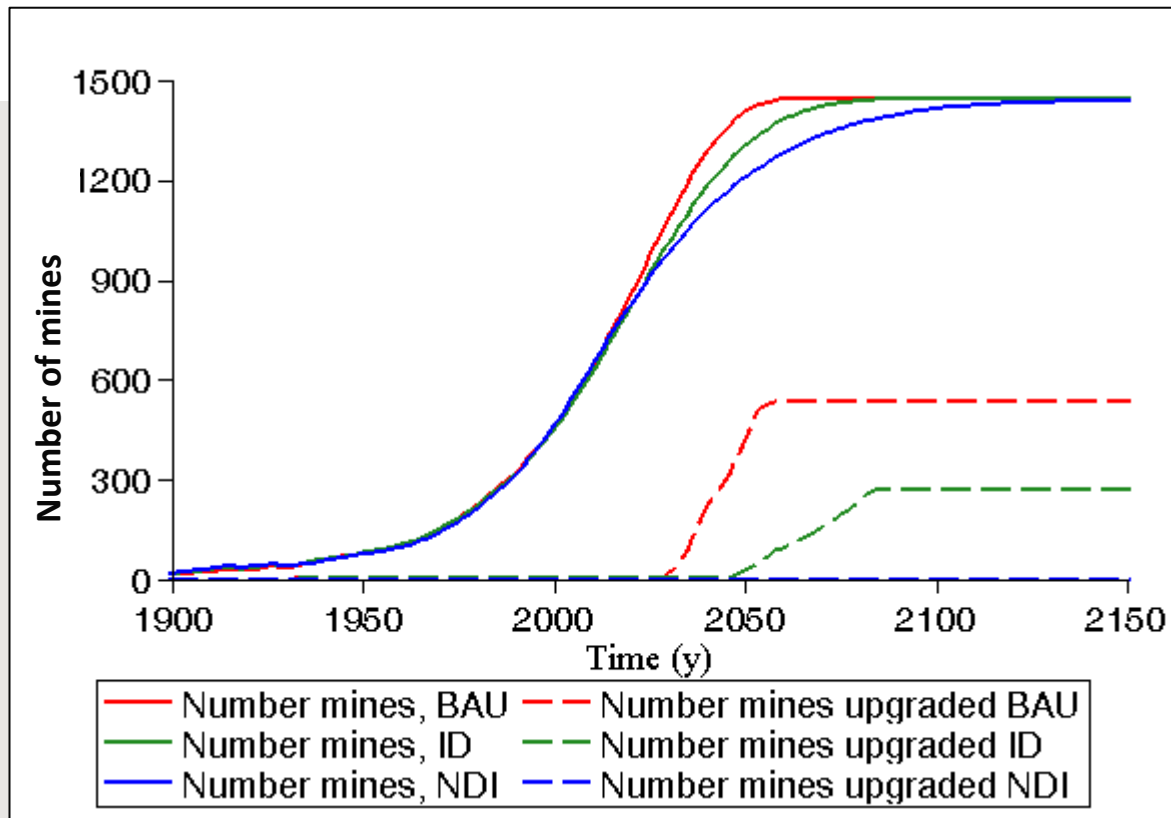
- Peak production takes place in 2066
- Intrinsic demand reduced well below BAU
- Supply curve is not symmetrical bell shape

# Effect of Different Demand Drivers



- Peak production BAU (2058), ID (2066), No DI (2055)
- For no demand influence supply curve is bell shaped

# Mines online and upgraded



- Number of mines brought online and upgraded increases with increasing demand scenario
- Increased pressure to discover new sources

# Conclusions



- Model, based on URR, regulates production from resource sources, to optimise demand-supply for a given market.
- Intrinsic demand can be modified to reflect resource depletion and supply limitations.
- Oceania Coal market peaks between 2055-2066 depending on demand influence.
- Increase rate of bringing mines online must be accompanied by greater exploration activity.

**More understanding is needed for demand influence**